

Contents lists available at ScienceDirect

Expert Systems With Applications



journal homepage: www.elsevier.com/locate/eswa

Air cargo load and route planning in pickup and delivery operations

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ARTICLE INFO

ABSTRACT

Dataset link: github.com/celiomesquita/ACLP_ RPDP_P

Keywords: OR in airlines Load planning Air palletization Weight and balance Pickup and delivery Vehicle routing In the aerial pickup and delivery of goods in a distribution network, transport aviation faces risks of load imbalance due to the urgency required for loading, immediate take-off, and mission accomplishment. Transport planners deal with trip itineraries, prioritization of items, building up pallets, and balanced loading, but there are no commercially available systems that can integrally assist in all these requirements. This enables other risks, such as improper delivery, excessive fuel burn, and possible safety issues due to cargo imbalance, as well as a longer than necessary turn-around time. This *NP-hard* problem, named *Air Cargo Load Planning with Routing, Pickup, and Delivery Problem (ACLP+RPDP)*, is mathematically modelled using standardized pallets in fixed positions. We developed a strategy to solve this problem, considering historical transport data from some Brazilian hub networks, and performed several experiments with a commercial solver, five known metaheuristics, and a new heuristic designed specifically for this problem. By using a portable computer, our strategy quickly found practical solutions to a wide range of real problems in much less than operationally acceptable time.

1. Introduction

The aviation industry adapts during global crises to keep supply chains moving. Air cargo provided complex expertise and the ability to access diverse destinations, delivering essential goods such as medicines, vaccine supplies, testing kits and other necessities with exceptional speed. This mode of transportation has become a preferred choice for governments, corporations and global companies in urgent need of transportation solutions.

Air cargo services are specially designed for organizations that require customized transportation, handle sensitive goods, or serve remote locations with limited routes. Air carriers typically use highcapacity cargo planes for economies of scale. Many cargo airlines have worldwide networks spread across destinations around the world.

A few years ago, Brandt and Nickel (2019) defined the Air Cargo Load Planning Problem (ACLPP) as four sub-problems: Aircraft Configuration Problem (ACP), Build-up Scheduling Problem (BSP), Air Cargo Palletization Problem (APP), and Weight and Balance Problem (WBP). Several aspects were considered: item characteristics to be transported (dimensions, scores, dangerousness, etc.); types and quantities of unit load devices (ULDs); when these pallets are assembled; how items are allocated to pallets; in which positions these pallets are to be placed; how total cargo weight is balanced; etc.

However, it is crucial to highlight that there are still other important challenges in air cargo transport that go beyond the definition of ACLPP, especially with regard to routes, and pickup and delivery at each destination. In this context, at least two more important subproblems can be considered: simultaneous pickup and delivery at each node, called the *Pickup and Delivery Problem* (PDP), and searching for the best benefit–cost route, which is a special case of the *Travelling Salesman Problem* (TSP).

Inefficient air transport plans can lead to unnecessary costs, extra routes, longer distances, and incorrect destinations. Unbalanced cargo increases fuel consumption due to altered aircraft pitch angles, increasing the risk of weight- and balance-related accidents. Balancing cargo is crucial for safe aerial transportation, as an improperly positioned centre of gravity (CG) can result in dangerous take-off and landing conditions and stall recovery issues. Despite technological advancements, many airlines still rely on manual aircraft loading and balancing, which can lead to flight delays. A rational decision-making process is essential to avoid creating inefficient or unsafe transport plans, considering high costs of fuel, maintenance, operation, outsourcing expenses, potential operational impairments, and safety risks due to unbalanced cargo. Solving this problem is vital for optimizing strategic scores, saving time and effort in loading, ensuring safety and balance, correct pickups and deliveries, and finding the best routes considering fuel use due to potential cargo imbalance.

The problem addressed in this work is the definition of the route of an aircraft that loads and unloads hundreds of items in several hubs, dealing with weight, volume, and balance constraints, and maximizing

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https://doi.org/10.1016/j.eswa.2024.123711

Received 13 December 2023; Received in revised form 28 February 2024; Accepted 17 March 2024 Available online 20 March 2024 0957-4174/© 2024 Elsevier Ltd. All rights reserved.

Distances between some Brazilian airports (*km*).

Source. www.anportuistanecearculator.com										
IATA ^a	GRU	GIG	SSA	CNF	CWB	BSB	REC			
GRU	0	343	1,439	504	358	866	2,114			
GIG	343	0	1,218	371	677	935	1,876			
SSA	1,439	1,218	0	938	1,788	1,062	676			
CNF	504	371	938	0	851	606	1,613			
CWB	358	677	1,788	851	0	1,084	2,462			
BSB	866	935	1,062	606	1,084	0	1,658			
REC	2,114	1,876	676	1,613	2,462	1,658	0			

^a International Air Transport Association.



Fig. 1. A route with 7 airports.

the benefit–cost ratio. This challenge has become even more acute during the COVID-19 pandemic due to the need for urgent medical supplies. Delays in shipping essential items such as respirators to critical areas highlighted the need for optimized solutions.

This problem is extremely complex, as it deals with different objectives: defining a route that visits all hubs; maximizing the items transported along this route, prioritizing the essential ones; making sure items reach the correct destinations; ensuring aircraft safety constraints; and saving fuel so that the flight is sustainable.

We have developed a heuristic process that can be run on a handheld computer, quickly providing a good solution to real instances of this problem. Solutions consist of flight itineraries, pickup and delivery plans, and the allocation of items onto pallets, ensuring the load-balancing constraints. Our method also reduces the stresses that transport planners are subject to, as they have to deal with extensive information in a short time frame.

To the best of our knowledge, this is the first time that an air cargo problem involving simultaneously APP, WBP, PDP, and TSP has been addressed. This new problem is named *Air Cargo Load Planning with Routing, Pickup, and Delivery Problem* (ACLP+RPDP). As we will describe in our mathematical modelling, these four sub-problems appear in an interconnected way in ACLP+RPDP and therefore cannot be solved independently.

As a real case study, we consider a crucial network for the *Brazilian Air Force*, as can be seen in Table 1 and Fig. 1. Although there are other airports of interest, these nodes were chosen due to their high demand. Other Brazilian airports tend to have smaller transport requests, which are generally met less expensively by cabotage, rail, or road transport.

This article is organized into six more sections. In Section 2, we make the literature review. In Section 3, we present the context and requirements of ACLP+RPDP. In Section 4, we describe its mathematical modelling. In Section 5, we describe the developed algorithms, whose results are presented in Section 6. Finally, our conclusions are in Section 7.

2. Literature review

The vast majority of operational research applied to air cargo is focused on challenges related to WBP, that is, the distribution of items on pallets to ensure load balancing. We can mention: Larsen and Mikkelsen (1980); Brosh (1981); Ng (1992); Heidelberg et al. (1998); Fok and Chun (2004); Kaluzny and Shaw (2009); Verstichel et al. (2011); Limbourg et al. (2012); Roesener and Barnes (2016); Chenguang et al. (2018); Zhao et al. (2021); Macalintal and Ubando (2023).

Other authors have addressed pallet assembly (APP) on aircraft, possibly also considering load balancing (WBP): Mongeau and Bes (2003); Chan et al. (2006); Roesener and Hall (2014); Vancroonenburg et al. (2014); Paquay et al. (2016, 2018); Wong and Ling (2020); Wong et al. (2021); Zhao et al. (2023).

In all these works, there is a great diversity of scenarios and solutions: some consider items in two dimensions, and others in three dimensions; some used integer programming, and others developed specific heuristics. Among the most recent, we can highlight:

- Roesener and Barnes (2016) proposed a heuristic to solve the *Dynamic Airlift Loading Problem* (DALP). Given a set of palletized cargo items that require transport between two nodes in a given time frame, the objective of this problem is to select an efficient subset of aircraft, partition the pallets into aircraft loads, and assign them to allowable positions in those aircraft.
- Paquay et al. (2016) presented a mathematical model to optimize the loading of heterogeneous 3D boxes on pallets with a truncated parallelepiped format. Its objective is to maximize the volume used in containers, considering load balancing constraints, the presence of fragile items, and the possibility of rotating these boxes. Paquay et al. (2018) developed some heuristics to solve this problem.
- Chenguang et al. (2018) modelled the air transport problem as a 2D packing problem and presented a heuristic for its optimization in several aircraft, considering load balancing to minimize fuel consumption.
- Wong and Ling (2020) developed a mathematical model and a tool based on mixed integer programming for optimizing cargo in aircraft with different pallet configurations. Balance constraints and the presence of dangerous items were considered. Wong et al. (2021) integrated this tool into a digital simulation model with a visualization and validation system based on sensors that alert about load deviations.
- Zhao et al. (2021) proposed a model for WBP based on Mixed Integer Programming (MIP). Instead of focusing on the CG deviation, the authors consider the original CG envelope of the aircraft, with a linearization method for its non-linear constraints.
- Zhao et al. (2023) presented three models that use integer programming for air cargo planning and weight balance optimization: bi-objective optimization (BOM), combinatorial optimization (COM), and enhanced combinatorial optimization (IOM). Considering a Boeing 777F in several scenarios, the tests revealed performance problems: BOM is fast, but produces large CG deviation; COM offers accurate optimization, but with impractical runtimes; IOM provides a balanced solution, improving speed over COM, but requiring high computational demands in some cases. Although IOM stands out for its effectiveness, all models face trade-offs between speed, accuracy and computational efficiency. This work alerted us to potential performance issues in solution methods.
- Macalintal and Ubando (2023) emphasized the proper selection of an aircraft, balancing factors such as cost, efficiency and limitations. These authors proposed a fuzzy linear programming model, which allows airlines to consider multiple objectives: maximizing payload, prioritizing specific items and minimizing operational costs. However, this approach does not take into account palletizing constraints.

Work	APP	WBP	PDP	TSP	2D	3D	Heu	Int	Lin
Larsen and Mikkelsen (1980)		*					*		
Brosh (1981)		*							*
Ng (1992)		*						*	
Heidelberg et al. (1998)		*			*		*		
Mongeau and Bes (2003)	*	*						*	
Fok and Chun (2004)		*						*	
Chan et al. (2006)	*					*	*		
Kaluzny and Shaw (2009)		*			*			*	
Verstichel et al. (2011)		*						*	
Limbourg et al. (2012)		*						*	
Roesener and Hall (2014)	*	*				*		*	
Vancroonenburg et al. (2014)	*	*						*	
Lurkin and Schyns (2015)		*	*					*	
Roesener and Barnes (2016)		*					*		
Paquay et al. (2016, 2018)	*	*				*	*	*	
Chenguang et al. (2018)		*			*		*		
Wong and Ling (2020)	*	*						*	
Wong et al. (2021)	*	*						*	
Zhao et al. (2021)		*						*	
Zhao et al. (2023)	*	*						*	
Macalintal and Ubando (2023)		*						*	
This article	*	*	*	*			*	*	

On the other hand, there are several works that address PDP (Bertsimas et al., 2019; Golestanian et al., 2023; Meng et al., 2023) or TSP (Ahmad et al., 2020; Cheikhrouhou & Khoufi, 2021; Debnath & Hawary, 2021; Xie et al., 2019) for unmanned aerial vehicles or aircraft, but none of them deal with APP and WBP.

Lurkin and Schyns (2015) is the only work that simultaneously addresses an air cargo (WBP) and a flight itinerary (PDP) sub-problem. The authors demonstrated that this problem is *NP-hard*. Although it is innovative, strong simplifications were imposed by these authors: in relation to loading, APP was ignored; regarding routing, it is assumed that a predefined tour plan is restricted to only two legs. Referring directly to this work, Brandt and Nickel (2019) comment: *However, not even these sub-problems are acceptably solved for real-world problem sizes, or models omit some practically relevant constraints.*

Table 2 lists the literature on air cargo transport with the subproblems involved. We also indicate whether the dimensions of the items were considered (2D or 3D) and which solution method was used: heuristic search methods (Heu), integer programming (Int), or linear programming (Lin).

As can be seen, none of these papers address air cargo palletization and load balancing with route optimization in a multi-leg transport plan for a single aircraft. Our work is the first to address a real air transport problem in which APP, WBP, PDP and TSP arise in an interconnected way.

3. Context and assumptions

In this section, we describe the context of the problem addressed in this work as well as the assumptions considered.

3.1. Operational premises

As we are dealing with an extremely complex and diverse problem, we decided to establish some simplifying characteristics:

- At each node of the tour, the items to be allocated are characterized by weight, volume, scores, and previously known destinations. We leave the consideration of 2D or 3D items to a future work.
- We considered a unique pallet type: the 463L Master Pallet, a common size platform for bundling and moving air cargo. It is the primary air cargo pallet for more than 70 Air Forces and many air transport companies. This pallet has a capacity of 4500 kg and 13.7 m³, which may be limited by its position along the



Fig. 2. A packed content on 463L pallet inside a Boeing C-17. Source: From Wikimedia Commons, the free media repository.

cargo bay. It is equipped for locking into cargo aircraft rail systems, and includes tie-down rings to secure nets and cargo loads, which in total weighs 140 kg. For more information, see www.463LPallet.com.

- All items allocated on a pallet must have the same destination. A
 pallet which has not yet reached its destination may receive more
 items, although it is known that these operations of removing
 restraining nets increase handling time and the risk of improper
 delivery. We do not consider oversized cargo in this work, but
 only cargo items that fit on these pallets.
- Finally, as we are interested in minimizing fuel costs, we disregarded others costs not directly associated with aircraft flight, such as handling.

Throughout this text, we call *packed content* (see Fig. 2) a set of items of the same destination stacked on a pallet and covered with a restraining net. It is considered a single item, having the same attributes as its components, whose values are the sum of individual scores, weights, and volumes. To ensure accuracy in pickup and delivery operations, packed content must remain on board until its destination.

	Payload: 75,000 kg			$limit_{long}^{CG}$: 1.170 m			$limit_{lat}^{CG}$: 0.19 m		
p_i	<i>p</i> ₁₇	<i>p</i> ₁₅	<i>p</i> ₁₃	<i>p</i> ₁₁	<i>p</i> 9	<i>p</i> ₇	<i>p</i> ₅	p_3	p_1
r1	<i>p</i> ₁₈	<i>p</i> ₁₆	p_{14}	<i>p</i> ₁₂	<i>p</i> ₁₀	p_8	p_6	p_4	p_2
plong ()	-17.57	-13.17	-8.77	-4.40	0	4.40	8.77	11.47	14.89
D_i^{long} (m)	-17.57	-13.17	-8.77	-4.40	0	4.40	8.77	11.47	14.89
D_i^{lat} (m)	1.32	1.32	1.32	1.32	1.32	1.32	1.32	1.32	1.32
$D_i^{(m)}$	-1.32	-1.32	-1.32	-1.32	-1.32	-1.32	-1.32	-1.32	-1.32
W_i (kg)	4,500	4,500	4,500	4,500	4,500	4,500	4,500	3,000	3,000
$V_i (m^3)$	14.8	14.8	14.8	14.8	14.8	14.8	14.8	10.0	7.0
Fuel cost	$c_d = US\$$	4.90/ <i>km</i>							
Fuel consumption rate	$c_{g} = 5\%$								
Maximum weight	$W_{max} = \sum_{i}$	$W_i = 75,000 \ k$	g						

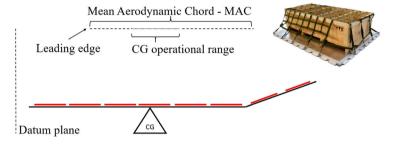


Fig. 3. Aircraft longitudinal cut, where red lines are pallets positions.

3.2. Aircraft parameters and load balancing

We consider real-world scenarios, where Table 3 shows the aircraft parameters. p_i are pallets, $1 \le i \le 18$, whose weight and volume limits are W_i and V_i , respectively. D_i^{long} and D_i^{lat} are, respectively, the longitudinal and lateral distances of each pallet centroids to the aircraft CG along both axes. These distances will be used in the calculation of the torque, referring to the items allocated on each pallet. In this aircraft, as the ramp has an inclination of 25°, we made the necessary corrections in D_i^{long} , W_i and V_i of the corresponding pallets (p_1 , p_2 , p_3 , and p_4).

This aircraft spends c_d dollars per kilometre flown and can carry up to W_{max} of cargo distributed on the pallets. The fuel penalty c_g is the percentage of cost increase due to the CG deviation on the longitudinal axis, estimated at 5.0%. It is important to consider that c_g tends to zero as the aircraft attitude tends to be level. As the CG deviation varies from 0 to $limit_{long}^{CG}$, this fuel penalty varies from 0 to c_g .

The torque applied to the aircraft must keep its CG in the operational range, which corresponds to a fixed percentage of the *Mean Aerodynamic Chord*¹ which is considered 1.17 m for the aircraft of this work (see Fig. 3).

We also make the following assumptions:

- on each pallet, the items are distributed in such a way that their CG coincides with the centroid of the pallet, because builders are well-trained to do so:
- the CG of the total load must be at a maximum longitudinal distance of *limit*^{CG}_{long} from the CG of the aircraft;
- the CG of the total load must be at a maximum lateral distance of *limit^{CG}* from the CG of the aircraft;
- the pallets are distributed in two identical rows (with odd and even indices, respectively), and the centroid of p_i is at a distance D^{lat}_i from the centreline of the aircraft;

• when there are items or packed contents in p_i , the common destination of this load will be assigned to variable T_i .

4. The mathematical modelling

In this section, we present the mathematical modelling of ACLP+RPDP in Tables 4, 5, 6, and 7, with their corresponding descriptions.

In Table 4, we describe the problem structure: nodes and their permutations, distances and associated costs, pallets characteristics, items available for shipment at each node, and packed contents shipped. The item *j* in node *k* has score s_j , weight w_j , volume v_j , and destination $to_j \in L_k$. Similarly, the packed content *q*, that remains on board at node *k*, has total weight w_q , total volume v_q , and destination $to_q \in L_k$. Packed contents that were destined to node *k* are unloaded when the aircraft arrives there; that is, they are not considered in Q_k .

Table 5 contains decision variables and the ACLP+RPDP allocation graph.

The calculus functions of ACLP+RPDP are described in Table 6.

$$\tilde{s}_{\pi} = \sum_{k=0}^{K} \sum_{i=1}^{m} \sum_{j=1}^{n_{\pi_{k}}} X_{ij}^{\pi_{k}} \times s_{j}$$

$$\tau_{\pi_{i}} = \sum_{k=0}^{m} \left[D_{i}^{long} \times \left(\sum_{j=1}^{n_{\pi_{k}}} X_{ij}^{\pi_{k}} \times w_{j} + \sum_{j=1}^{m_{\pi_{k}}} Y_{ij}^{\pi_{k}} \times w_{j} \right) \right] / W_{max} \times limit_{lows}^{CG};$$
(1)

$$\tau_{\pi_k} = \sum_{i=1}^{k} \left[D_i^{-0} \times \left(\sum_{j=1}^{k} X_{ij}^{-1} \times w_j + \sum_{q=1}^{k} Y_{iq}^{-1} \times w_q \right) \right] / w_{max} \times limit_{long}^{-1};$$

$$k \in \{0, -K\}$$
(2)

$$\tilde{c}_{-} = \sum_{k=1}^{K} \left[c_{-k} + c_{-k} \times |\tau_{-k}| \right]$$
(3)

$$L_{\pi_k} = L_{\pi_{k-1}} - \{\pi_k\}; \ k \in \{1, \dots, K\}$$
(4)

$$\epsilon_{\pi_k}^t = \sum_{i=1}^m \left[D_i^{lat} \times \sum_{j=1}^{n_{\pi_k}} \left(X_{ij}^{\pi_k} \times w_j \times (i\%2) - X_{ij}^{\pi_k} \times w_j \times (i+1)\%2 \right) \right] / W_{max} \times limit_{lat}^{CG}$$
(5)

¹ Chord is the distance between the leading and trailing edges of the wing, measured parallel to the normal airflow over the wing. The average length of the chord is known as the *Mean Aerodynamic Chord* (MAC).

Notation	Description
$L = \{0, 1, \dots, K\}$	Set of $K + 1$ nodes of the tour, where node 0 is the base
π	A permutation between nodes 1,, K
S _K	Set of K! permutations
π_k	The <i>k</i> th node of tour π , $1 \le k \le K$
Tour <i>π</i>	$\{0, \pi_1, \dots, \pi_K, 0\}$ For ease of notation, $\pi_0 = \pi_{K+1} = 0$
L_k	Set of remaining nodes of tour at node $k, 0 \le k \le K$ By definition, $L_0 = L$
d(a,b)	Distance from node <i>a</i> to node <i>b</i> , where $0 \le a, b \le K$ By definition, $d(a, a) = 0, \forall a$
$C = \begin{bmatrix} c_{a,b} \end{bmatrix}$	Cost matrix of flights, where $c_{a,b} = c_d \times d(a, b)$
$M = \{1, \dots, m\}$	Set of <i>m</i> pallets in specific positions within the aircraft See Table 3, where $m = 18$
$N_k = \{1, \dots, n_k\}$	Set of n_k items available for loading at node k , $1 \le j \le n_k$, $0 \le k \le R$
$N = \bigcup_{0 \leq k \leq K} N_k$	Set of items in all nodes along a tour
$Q_k = \{1, \dots, m_k\}$	Set of $m_k \le m$ packed contents at node k , $1 \le q \le m_k$, $0 \le k \le K$ By definition, $m_0 = 0$ and $Q_0 = \emptyset$

_

Decision variables and allocation graph.

N	
Notation	Description
$\begin{array}{l} X_{ij}^{\pi_k} {\rm and} Y_{iq}^{\pi_k} \\ X_{ij}^{\pi_k} = 1 \\ Y_{iq}^{\pi_k} \in L \\ T_i^{\pi_k} \in L_{\pi_k} \end{array}$	Binary variables, where $1 \le i \le m$, $1 \le j \le n_{\pi_k}$, $1 \le q \le m_{\pi_k}$ and $0 \le k \le K$
$X_{ii}^{\pi_k} = 1$	If item j at node π_k is assigned to pallet i, and 0 otherwise
$Y_{iq}^{\vec{\pi}_k} = 1$	If packed content q at node π_k is assigned to pallet i, and 0 otherwise
$T_i^{\pi_k} \in L_{\pi_k}$	Destination of items and packed contents assigned to pallet i at node π_k
$G_{\pi_k}(V_{\pi_k}, E_{\pi_k})$	Allocation graph at node π_k
$V_{\pi_k} = M \cup N_{\pi_k} \cup Q_{\pi_k}$	Allocation graph vertices at node π_k : pallets, items and packet contents
$E_{N_{x_{k}}}$	Allocation graph edges at node π_k , corresponding to shipped items
$E_{Q_{x_{i_{*}}}}$	Allocation graph edges at node π_k , corresponding to packed contents
$E_{\pi_k} = E_{N_{\pi_k}} \cup E_{Q_{\pi_k}}$	Allocation graph edges at node π_k
$(i,j) \in E_{N_{\pi_{l}}}$	If $X_{ij}^{\pi_k} = 1$, where <i>i</i> is a pallet and <i>j</i> is a item at node π_k
$(i,q) \in E_{Q_{\pi_k}}$	If $Y_{iq}^{\bar{\pi}_k} = 1$, where <i>i</i> is a pallet and <i>q</i> is a packed content at node π_k

$$\epsilon_{\pi_{k}}^{a} = \sum_{i=1}^{m} \left[D_{i}^{lat} \times \sum_{q=1}^{m_{\pi_{k}}} \left(Y_{iq}^{\pi_{k}} \times w_{q} \times (i\%2) - Y_{iq}^{\pi_{k}} \times w_{q} \times (i+1)\%2 \right) \right] / W_{max} \times limit_{lat}^{CG}$$
(6)

Table 6

т

Calculus functions.						
Function	Description					
(1)	Total score of transported items throughout tour π					
(2)	Longitudinal torque applied by loaded pallets at node π_k					
(3)	Total cost of fuel on tour π (distances and CG longitudinal deviations)					
(4)	Set of not visited nodes at node π_k					
(5)	Lateral torque at node π_k (shipped items)					
(6)	Lateral torque at node π_k (packed contents)					
(7)	Objective function of ACLP+RPDP					

$$\max_{\pi \in S_K} f_{\pi} = \tilde{s}_{\pi} / \tilde{c}_{\pi}$$
(7)

Longitudinal (2) and lateral torques ((5), (6)) are calculated in proportion to the highest torque supported by the aircraft. As there are two rows of pallets, one on each side of the centreline, we use the operator *modulo* (%) to calculate lateral torques. In our experiments, we found that the magnitude of these lateral torques was always minimal, so we decided to ignore them in the fuel consumption (3). The objective of ACLP+RPDP (7) is to find a permutation $\pi \in S_K$ with the corresponding allocation of items on pallets at each node that maximizes the function $f_{\pi} = \tilde{s}_{\pi}/\tilde{c}_{\pi}$.

Finally, ACLP+RPDP constraints related to each node π_k are described in Table 7.

$$|\tau_{\pi_{k}}| \le 1; \ k \in \{0, \dots, K\}$$
 (8)

$$|\epsilon_{\pi_k}^t + \epsilon_{\pi_k}^a| \le 1 \tag{9}$$

$$\sum_{j=1}^{n_{\pi_k}} X_{ij}^{\pi_k} \times w_j + \sum_{q=1}^{m_{\pi_k}} Y_{iq}^{\pi_k} \times w_q \le W_i; \ i \in \{1, \dots, m\}$$
(10)

$$\sum_{j=1}^{n_{\pi_k}} X_{ij}^{\pi_k} \times v_j + \sum_{q=1}^{m_{\pi_k}} Y_{iq}^{\pi_k} \times v_q \le V_i; \ i \in \{1, \dots, m\}$$
(11)

$$\sum_{i=1}^{m} X_{ij}^{\pi_k} \le 1; \ j \in \{1, \dots, n_{\pi_k}\}$$
(12)

$$\sum_{i=1} Y_{iq}^{\pi_k} = 1; \ to_q \in L_{\pi_k}; \ q \in \{1, \dots, m_{\pi_k}\}$$
(13)

$$X_{ij}^{\pi_k} <= X_{ij}^{\pi_k} \times (T_i^{\pi_k} - to_j + 1); \ i \in \{1, \dots, m\}; \ j \in \{1, \dots, n_{\pi_k}\}$$
(14)

$$X_{ij}^{\pi_k} \le X_{ij}^{\pi_k} \times (to_j - T_i^{\pi_k} + 1); \ i \in \{1, \dots, m\}; \ j \in \{1, \dots, n_{\pi_k}\}$$
(15)

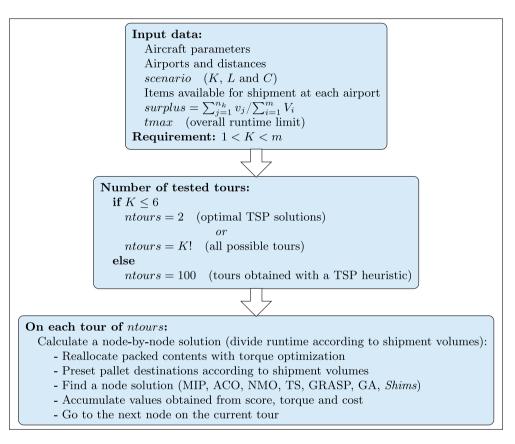
$$Y_{iq}^{\pi_k} <= Y_{iq}^{\pi_k} \times (T_i^{\pi_k} - to_q + 1); \ i \in \{1, \dots, m\}; \ q \in \{1, \dots, m_{\pi_k}\}$$
(16)

$$Y_{iq}^{\pi_k} <= Y_{iq}^{\pi_k} \times (to_q - T_i^{\pi_k} + 1); \ i \in \{1, \dots, m\}; \ q \in \{1, \dots, m_{\pi_k}\}$$
(17)

Once the assumptions and the mathematical modelling are presented, it is possible to see that ACLP+RPDP is *NP*-hard. In a similar way to Lurkin and Schyns (2015), consider the simple case where K = 1 (one leg), m = 2 (two pallets around the aircraft CG), 2n sufficiently light

Table 7	
Constraints.	
Constraint	De

Constraint	Description
((8), (9))	Longitudinal and lateral torques must be within aircraft limits
((10), (11))	Items allocated to each pallet cannot exceed its weight and volume limits
(12)	At most, each item is associated with a single pallet
(13)	Packed contents that have not yet reached their destination must remain on board
((14), (15))	Items allocated on the same pallet must have the same destinations
((16), (17))	If there is a packed content on the pallet, it must also have the same destination as other items





items with same scores in node 0, and no items in node 1. Under these conditions, through polynomial reductions for the *Set-Partition Problem*, it is possible to demonstrate that the decision problem associated with ACLP+RPDP is *NP-complete*. For more details, see Lurkin and Schyns (2015, p. 6).

5. Solution process

Throughout our research, we have thoughtfully described ACLP+RPDP in standard MIP format and found that no solver can handle its practical cases in a feasible time. Thus, as ACLP+RPDP is highly complex, involving four intractable and interconnected sub-problems, we decided to focus on *real cases*, developing quick node-by-node solutions, not necessarily optimal, but which would allow us to obtain a complete tour.

In practical cases, we know that a common aircraft has m = 18 pallets, flight itineraries have $K \le 6$ nodes plus the base, and each node has hundreds of items to be shipped. We also know that missions with fewer nodes are more frequent than longer ones. Under these circumstances, we can adopt some important strategies summarized in Fig. 4:

• We consider that the number of destinations is smaller than the number of pallets (K < m), and we avoid the trivial case where

K = 1. With this premise, we can preset the destinations of the pallets at each shipping node, reserving a number of pallets proportional to the volume available for each destination. We could have used another criterion, but it was observed in the experiments that the volume is more constrictive in airlift.

- An important parameter is the number *ntours* of tours tested. In practical cases where $K \leq 6$, we have the possibility to check all possible tours (*ntours* = K!). In this situation, as K is small, we can also specially analyse the two optimal solutions of the corresponding TSP (*ntours* = 2). Finally, in cases where K > 6, we will use a heuristic to select 100 tours of low length (*ntours* = 100), and search among them for the one that provides the best value for the objective function.
- To compare the performance of each strategy, an overall runtime limit *tmax* is established and divided by *ntours* tours. In turn, the runtime limit for each tour will be distributed among its nodes in proportion to the volume available for boarding.
- At each node of a tour, the packed contents that remain on board are reallocated on pallets in order to minimize torque on the aircraft. This calculation is done quickly using a MIP solver. Then, the destinations of the pallets are previously defined in proportion to the shipment volume. Finally, considering the runtime limit of each node, we will use a MIP solver and five well-known meta-heuristics to find the best allocation of shipping items: *Ant*

Table 8

Testing scenario	os.	
Scenario	K	L
1	2	{0,1,2}
2	3	$\{0, 1, 2, 3\}$
3	4	$\{0, 1, 2, 3, 4\}$
4	5	$\{0, 1, 2, 3, 4, 5\}$
5	6	$\{0, 1, 2, 3, 4, 5, 6\}$

Colony Optimization (ACO), Noising Method Optimization (NMO), Tabu Search (TS), Greedy Randomized Adaptive Search Procedure (GRASP), and Genetic Algorithm (GA). We will also introduce a very fast heuristic, developed specifically for this problem, called Shims.

- · We will generate benchmarks using the surplus parameter, which is a value in $\{1.2, 1.5, 2.0\}$. It corresponds, at each node k, to the ratio between the sum of the volumes of the items and the load capacity of the pallets (*surplus* = $\sum_{j=1}^{n_k} v_j / \sum_{i=1}^{m} V_i$). This parameter allows us to verify the different behaviour of each method, according to scenario and the quantity of items available for shipment.
- We will do tests by varying the number K of destinations, the set L of nodes, and the costs C. Each group of values tested is called scenario, according to Tables 1 and 8, where $1 < K \leq 6$. After finding the method with the best performance in node-by-node solution, we will test it in solving cases with K > 6.

Algorithm 1 is the main program of this solution process, which parameters are scenario, surplus, tmax, and ntours. The input data is obtained from Tables 1, 3 and 8 (lines 2-3).

Algorithm 1 Solving ACLP+RPDP
1: ACLP+RPDP in: scenario, surplus, tmax, ntours out: answer
2: Let M be the set of pallets (<i>cfr.</i> Table 3)
3: Let K, L and C be according to the scenario (cfr. Tables 1, 3 and 8)
4: $N \leftarrow ItemsGeneration(scenario, surplus)$
5: for each method do
6: for $i \leftarrow 1$ to neous do
7: $f_i \leftarrow SolveTour(\pi[i], L, M, C, N, method, tmax/ntours)$
8: end for
9: answer[scenario, surplus, method] $\leftarrow \max f_i$
10: end for

surplus is passed to ItemsGeneration (line 4), responsible for creating the items to be shipped, which will be presented in the next section (Algorithm 7). *tmax* is the runtime limit, which will be distributed among the tours (line 7). method corresponds to a MIP solver or a heuristic to the node-by-node solution SolveTour, which will be presented in Section 5.2. The best results obtained by testing all tours are stored in answer (line 9), which is the output of this algorithm.

 π [] is a vector of tours indexed from 1 to *ntours*. When *ntours* = 2, $\pi[1]$ and $\pi[2]$ are the optimal solutions of the corresponding TSP. When *ntours* = K!, $\pi[i]$ is the *i*th permutation of S_K . Finally, when *ntours* = 100, π [1], ..., π [100] are the solutions provided by a TSP heuristic.

Next, we will present two subsections: in the first we explain how SolveTour is executed. In the second we will present the heuristics developed for node-by-node solutions.

5.1. SolveTour algorithm

As we commented in the previous subsection, we will adopt the strategy of presetting the destinations of each pallet throughout the tour. This is feasible in practical cases where 1 < K < m. For this, each pallet *i* also has a field T_i^k , $0 \le k \le K$, which stores its next destination after being loaded at node k. For this reason, $T_i^k \in L_k$, $1 \le i \le m$, $0 \le k \le K$.

SolveTour is described in Algorithm 2, where π is a permutation of the nodes (excluding the base) that defines the order of visits in this tour, method corresponds to a MIP solver or a heuristic for solving the node-by-node problems, and *tmax* is the runtime limit of this tour.

Algorithm 2 Solving tour π with *method*

- 1: SolveTour in: π , L, M, C, N, method, tmax out: score/cost
- 2: $\pi_0 \leftarrow 0$ \triangleright all tours start and end at the base

3: $\pi_{K+1} \leftarrow 0$

4: score $\leftarrow 0$ 5: $cost \leftarrow 0$

- 6: for $k \leftarrow 0$ to K do
- $t_{\pi_k} = (\sum_{j=1}^{n_k} v_j / \sum_{k=0}^{K} \sum_{j=1}^{n_k} v_j) * tmax$ 7: ▷ runtime limit proportional to the shipment volume
- $L_{\pi_k} \leftarrow L \{\pi_0, \pi_1, \dots, \pi_k\}$ $T_i^{\pi_k} \leftarrow -1, \ 1 \le i \le m$ 8: ▷ the set of remaining nodes is updated 9: ▷ the pallet destination is unset
- 10: if k = 0 then

11:

Let $G_1(M \cup N_0, \emptyset)$ ▷ no packed contents at the base else

12: $E_{Q_{\pi_k}}, M \leftarrow UpdatePacked(M, Q_{\pi_k}, \pi_k)$ 13:

14: Let $G_1(M \cup N_{\pi_k} \cup Q_{\pi_k}, E_{Q_{\pi_k}})$

15: end if

 $M \leftarrow SetPalletsDestinations(M, \pi_k)$ 16:

 $G_2 \leftarrow SolveNode(method, \pi_k, G_1, t_{\pi_k})$ 17:

 $s, \tau \leftarrow ScoreAndTorque(\pi_k, G_2)$ 18:

19: $score \leftarrow score + s$

20: $cost \leftarrow cost + c_{\pi_k,\pi_{k+1}} \times (1 + c_g \times |\tau|)$ 21: end for

As we mentioned in the previous section, all tours start and end at the base 0 (lines 2-3). After initializing the score and cost values (lines 4–5), there is a loop for the K + 1 flights (lines 6–21). Initially, the runtime limit t_{π_k} for each node is calculated (line 7), the set L_{π_k} of remaining nodes is updated (line 8), and the pallet destinations are unset (line 9).

When the aircraft is at the base, the initial graph G_1 is empty, and there are no packed contents (line 11). Otherwise, UpdatePacked (line 13) returns the set of packed contents that have not yet reached their destination and remain on board, rearranging them on the pallets to minimize CG deviation. This allocation is stored in graph G_1 (line 14).

SetPalletsDestinations (line 16) presets the destination of each pallet based on the volume demands of the current node without changing the pallet's destination with packed contents.

Finally, SolveNode includes the edges corresponding to the items shipped at the current node, returning the graph G_2 (line 16). The score and the CG deviation of G_2 are calculated (line 18) and accumulated (lines 19-20), allowing the final result of this tour as output.

UpdatePacked, described in Algorithm 3, finds the best packedpallet allocation, in terms of CG deviation, for the packed contents that remain on board.

Algorithm 3	3	Updating	the	packed	contents	that	remain	boarded	at
node π_k									

1: UpdatePacked in: M, Q_{π_k}, π_k out: $E_{Q_{\pi k}}$, M 2: $E_{Q_{\pi_k}} \leftarrow MinCGDeviation(E_{Q_{\pi_k}})$ 3: for $i \leftarrow 1$ to m do 4: for $q \leftarrow 1$ to m_{π_k} do $T_{:}^{\pi_{k}} \leftarrow -1$ 5: if $(i,q) \in E_{Q_{\pi_k}}$ then 6: $T_{:}^{\pi_{k}} \leftarrow to_{q}$ 7: ▷ reassign pallet destinations end if 8: 9 end for 10: end for

MinCGDeviation (line 2) relocates the packed contents on the pallets, minimizing torque and ensuring that they all remain on board, one packed content on each pallet. It is run through a MIP solver with the objective function (18) and the constraints (19) and (20). As there are few variables, $E_{Q_{\pi_k}}$ is obtained in less than 30 milliseconds. Finally, the destination of each pallet with packed content is updated (lines 3–10).

$$\min f = \Big| \sum_{i=1}^{m} \sum_{q=1}^{m_{\pi_k}} Y_{iq}^k \times w_q \times D_i^{long} \Big|$$
(18)

$$\sum_{i=1}^{m} Y_{iq}^{k} = 1; \ q \in \{1, \dots, m_{\pi_{k}}\}$$
(19)

$$\sum_{q=1}^{m_{\pi_k}} Y_{iq}^k \le 1; \ i \in \{1, \dots, m\}$$
(20)

SetPallets Destinations, which sets the pallets destination not yet defined, is described in Algorithm 4.

Algorithm 4 Setting pallets destination based on the items to be embarked at node π_k

ĸ
1: SetPalletsDestinations in: M, π_k out: M
2: $vol_x \leftarrow 0, x \in L_{\pi_k}$
3: $max \leftarrow 0$ \triangleright destination with maximum volume demand
4: $total \leftarrow 0$
5: for $j \leftarrow 1$ to n_{π_k} do
6: if $to_j \in L_{\pi_k}$ then
7: $vol_{to_i} \leftarrow vol_{to_i} + v_j$
8: $total \leftarrow total + v_j$
9: if $vol_{to_i} > vol_{max}$ then
10: $max \leftarrow to_j$
11: end if
12: end if
13: end for
14: for $x \in L_{\pi_k}$ do
15: if $vol_x \neq 0$ then
16: $needed \leftarrow \max\{1, \lfloor (m - m_{\pi_k}) \times vol_x / total \rfloor\}$
17: $np \leftarrow 0$
18: for $i \leftarrow 1$ to m do
19: if $(np < needed)$ and $(T_i^{\pi_k} = -1)$ then
$20: T_i^{\pi_k} \leftarrow x$
21: $np \leftarrow np + 1$ \triangleright number of necessary pallets to node x
22: end if
23: end for
24: end if
25: end for
26: for $i \leftarrow 1$ to m do
27: if $T_i^{\pi_k} \leftarrow -1$ then
28: $T_i^{\pi_k} \leftarrow max \qquad \triangleright$ any remaining pallet is assigned to the maximum
demand destination
29: end if
30: end for

vol stores the demand volume of items destined for the non-visited nodes (line 2). The destination of empty pallets is defined proportionally to the volume of items to be embarked (lines 14–25). *max* is the destination with maximum volume demand (line 10), and *needed* is the number of necessary pallets to node x (line 16). The destination with the maximum volume defines any remaining pallets (lines 26–30).

ScoreAndTorque, described in Algorithm 5, evaluates the allocation graph *G* generated by *SolveNode* at node π_k and returns the corresponding cargo score and aircraft torque.

Algorithm 5 consists of a loop that goes through all the pallets (lines 5–18), accumulating the scores (lines 8 and 14) and the torques (lines 9 and 15) of the shipped items, allowing the final calculation of the aircraft torque (line 19).

5.2. Node-by-node solutions

In this subsection, we present two implementations of *SolveNode* algorithm: with a MIP solver and with heuristics.

Algorithm 5 Cargo score and aircraft	torque
1: ScoreAndTorque in: π_k , G out: s,	τ
2: Let $G(V_{\pi_k}, E_{Q_{\pi_k}} \cup E_{N_{\pi_k}})$	
3: $s \leftarrow 0$	
4: $\tau_i \leftarrow 0, \ 1 \le i \le m$	
5: for $i \leftarrow 1$ to m do	
6: for $j \leftarrow 1$ to n_{π_k} do	
7: if $X_{ij}^{\pi_k} = 1$ then	
8: $s \leftarrow s + s_j$	▷ accumulates cargo score
9: $\tau_i \leftarrow \tau_i + w_i \times D_i^{long}$	▷ accumulates aircraft torque
10: end if	
11: end for	
12: for $q \leftarrow 1$ to m_{π_k} do	
13: if $Y_{iq}^{\pi_k} = 1$ then	
14: $s \leftarrow s + s_q$	▷ accumulates cargo score
15: $\tau_i \leftarrow \tau_i + w_q \times D_i^{long}$	▷ accumulates aircraft torque
16: end if	
17: end for	
18: end for	
19: $\tau \leftarrow \sum_{i=1}^{m} \tau_i / (W_{max} \times limit_{long}^{CG}) \qquad \triangleright \text{ fin}$	hal calculation of the aircraft torque

5.2.1. Node-by-node solutions with a MIP solver

Our strategy adopted in *SolveTour* defines the values of some variables: the set of nodes to be visited is updated, the packed contents that remain on board are reallocated to minimize the CG deviation, and the pallet's destinations are determined according to the volume of items available for shipment.

In this way, the mathematical model for *SolveNode* (*MIP*, π_k , *G*, *tmax*) becomes simpler, which finds an allocation of available items at node π_k using previously defined values of L_{π_k} , $T_i^{\pi_k}$, and $a_q^{\pi_k}$. Thus, we use a MIP solver with a runtime limit *tmax* at node π_k to maximize the objective function (21) with the calculus Eqs. (22) to (24), subject to the constraints (25) to (31). The binary variables X_{ij} and Y_{iq} define the sets of edges $E_{N_{\pi_k}}$ and $E_{Q_{\pi_k}}$, respectively, included in graph *G*.

$$\max f = \tilde{s}/\tilde{c} \tag{21}$$

$$S = \sum_{i=1}^{m} \sum_{j=1}^{n_{\pi_k}} X_{ij} \times s_j$$
(22)

$$\tau_{\pi_k} = \sum_{i=1}^{m} \left[D_i^{long} \times (\sum_{j=1}^{n_{\pi_k}} X_{ij} \times w_j + \sum_{q=1}^{m_{\pi_k}} Y_{iq} \times w_q) \right] / W_{max} \times limit_{long}^{CG}$$
(23)

$$\tilde{c} = c_{\pi_k,\pi_{k+1}} \times (1 + c_g \times |\tau_{\pi_k}|)$$
(24)

$$\tau_{\pi_k}| \le 1 \tag{25}$$

$$\sum_{j=1}^{n_{\pi_k}} X_{ij} \times w_j + \sum_{q=1}^{m_{\pi_k}} Y_{iq} \times w_q \le W_i; \ i \in \{1, \dots, m\}$$
(26)

$$\sum_{j=1}^{n_{\pi_k}} X_{ij} \times v_j + \sum_{q=1}^{m_{\pi_k}} Y_{iq} \times v_q \le V_i; \ i \in \{1, \dots, m\}$$
(27)

$$\sum_{i=1}^{m} X_{ij} \le 1; \ j \in \{1, \dots, n_{\pi_k}\}$$
(28)

$$X_{ij} = 0; \ to_j \notin L_{\pi_k}; \ i \in \{1, \dots, m\}; \ j \in \{1, \dots, n_{\pi_k}\}$$
(29)

$$X_{ij} \le X_{ij} \times (T_i^{\pi_k} - to_j + 1); \ i \in \{1, \dots, m\}; \ j \in \{1, \dots, n_{\pi_k}\}$$
(30)

$$X_{ij} \le X_{ij} \times (to_j - T_i^{\pi_k} + 1); \ i \in \{1, \dots, m\}; \ j \in \{1, \dots, n_{\pi_k}\}$$
(31)

The constraints (30) and (31) are equivalent to $X_{ij} = 1$ if $to_j = T_i^{\pi_k}$, and $X_{ij} = 0$ otherwise.



Fig. 5. Shims of various thicknesses. Source: www.mscdirect.com/product /details/70475967

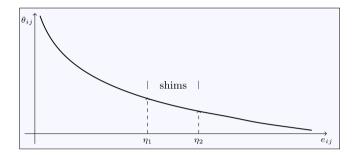


Fig. 6. n_{π_i} possible edges e_{ij} sorted by θ_{ij} in non-ascending order.

5.2.2. Node-by-node solutions with heuristics

One of the main objectives of this work was to find a quick heuristic that offers a good-quality solution for the node-by-node problem. Taking this into account, we design algorithms based on five known meta-heuristics: Ant Colony Optimization (ACO) (Dorigo, 1992; Dorigo et al., 1996), Noising Method Optimization (NMO) (Charon & Hudry, 1993, 2001; Zhan et al., 2020), Tabu Search (TS) (Glover, 1986), Greedy Randomized Adaptive Search Procedure (GRASP) (Feo & Resende, 1989), and Genetic Algorithm (GA) (Holland, 1992). We considered several ideas from the literature (Alonso et al., 2019; Fidanova, 2006; Niar & Freville, 1997; Peerlinck & Sheppard, 2022; Zhan et al., 2020), and we were careful to use the same data structures and procedures in all implementations to enforce fair results comparison.

However, the heuristic that presented better solutions was none of the previous ones. In this subsection, we will present a new heuristic for the node-by-node problem, called Shims. Like in mechanics, shims are collections of spacers to fill gaps, which may be composed of parts with different thicknesses (see Fig. 5). This strategy is based on a practical observation: usually, subsets of smaller and lighter items are saved for later adjustments to the remaining available space.

The selection of edges for $E_{N_{\pi}}$ uses the edge attractiveness θ_{ij} (32), which can be understood as the tendency to allocate item j to pallet iat node π_k . It is directly proportional to the score, and inversely to the volume and the torque of each item.

$$\theta_{ij} = \frac{s_j}{v_j} \times \left(1 - \frac{w_j \times |D_i^{long}|}{\max w_j \times \max |D_i^{long}|}\right); \ i \in \{1, \dots, m\}, \ j \in \{1, \dots, n_{\pi_k}\}$$
(32)

Considering only the items that can be shipped at node π_k , Fig. 6 represents n_{π_k} possible edges e_{ij} of pallet *i* sorted by θ_{ij} in nonascending order. Initially, Shims builds a greedy solution for pallet *i* selecting edges up to index η_1 (greedy phase). Then, with the edges between η_1 and η_2 , it elaborates different possible complements (composition phase), including later the best ones in the same pallet (selection phase). Shims is depicted in Algorithm 6.

- **Algorithm 6** *Shims* heuristic at node π_k 1: SolveNode in: Shims, π_k , G, tmax, level₁, level₂ out: $G(M \cup N_{\pi_k} \cup$ $Q_{\pi_k}, E_{Q_{\pi_k}} \cup E_{N_{\pi_k}})$ 2: $T_{begin} \leftarrow$ current system time 3: Let $G(M \cup N_{\pi_k} \cup Q_{\pi_k}, E_{Q_{\pi_k}})$ 4: Sort M by $|D_i^{long}|$ in non-descending order 5: $E_{N_{\pi_k}} \leftarrow \emptyset$ 6: $\tau_{max} \leftarrow W_{max} \times limit_{long}^{CG}$ 7: for $i \leftarrow 1$ to m do $\tau_{\pi_k} \leftarrow \sum_{(i,q) \in E_{Q_{\pi_k}}} w_q \times D_i^{long}$ 8: $vol_i \leftarrow \sum_{(i,q) \in E_{Q_{\pi_k}}} v_q$ 9: Let *E* be an array of n_{π_k} possibles edges of pallet *i* sorted by θ_{ij} in 10: non-ascending order 11: $\eta_1 \leftarrow 1$ 12: repeat 13: $e_{ij} \leftarrow E_{\eta_i}$ if $(E_{N_{\pi_i}} \cup \{e_{ij}\}$ is feasible) and $(vol_i \leq V_i \times level_1)$ and $(|\tau_{\pi_k} + w_j \times level_1)$ 14: $|W_{max} \times limit_{long}^{CG}$ then D^{l} $\begin{array}{l} E_{N_{\pi_k}} \leftarrow E_{N_{\pi_k}} \cup \{e_{ij}\} \\ vol_i \leftarrow vol_i + v_j \end{array}$ 15: 16: 17: $\tau_{\pi_k} \leftarrow \tau_{\pi_k} + w_j \times D_i^{long}$ 18: $\eta_1 \leftarrow \eta_1 + 1$ 19: end if 20: until $(vol_i > V_i \times level_1)$ or $(\eta_1 > n_{\pi_i})$ 21: $slack_i \leftarrow V_i - vol_i$ 22: $\eta_2 \leftarrow \eta_1$ 23: while $(\eta_2 \leq n_{\pi_k})$ and $(vol_i < V_i \times level_2)$ do 24: $e_{ij} \leftarrow E_{\eta_2}$ 25: $vol_i \leftarrow vol_i + v_i$
- 26: $\eta_2 \leftarrow \eta_2 + 1$
- 27: end while
- 28:
- $vol \leftarrow 0; b \leftarrow 1; shims_b \leftarrow \emptyset; Set \leftarrow \{shims_b\}$ 29:
- **for** $x \leftarrow \eta_1$ to η_2 **do** 30: if $T_{current} - T_{begin} > tmax$ then
- 31: break
- 32: end if
- 33: $NewShims \leftarrow True$
- 34: $e_{ii} \leftarrow E_x$
- 35: for $shims \in Set$ do
- 36: if $(e_{ij} \notin (E_{N_{\pi_k}} \cup shims))$ and $(e_{ij} \text{ is feasible})$ and $((v_j + vol) \leq$ slack.) then
- 37: shims \leftarrow shims $\cup \{e_{ij}\}$
- 38. $vol \leftarrow vol + v_i$ 39:
- 40: break
- end if 41: 42:
 - end for
- 43: if NewShims then
- $vol \leftarrow 0; b \leftarrow b+1; shims_b \leftarrow \{e_{ij}\}$ 44: 45:
 - $Set \leftarrow Set \cup \{shims_h\}$
- 46: end if 47:
 - end for
- $sh_w \leftarrow shims$, where $shims \in Set$ and $\sum_{e_{ij} \in shims} w_j$ is maximum $sh_v \leftarrow shims$, where $shims \in Set$ and $\sum_{e_{ij} \in shims} v_j$ is maximum 48: 49:
- $sh_{best} \leftarrow shims$, where $shims \in \{sh_w, sh_v\}$ and $\sum_{e_{ij} \in shims} s_j$ is maximum 50: 51: $E_{N_{\pi_{k}}} \leftarrow E_{N_{\pi_{k}}} \cup sh_{best}$ 52: end for

tmax is the runtime limit for *Shims*, and $level_1$ and $level_2$ are volume thresholds for indices η_1 and η_2 , respectively. Initially, Q_{π_k} (line 3) corresponds to the packed contents that remain on board. It is important to remember that $E_{\mathcal{Q}_{\pi_k}}$ and M were modified by the procedure $UpdatePacked(M, Q_{\pi_k}, \pi_k)$ and the procedure SetPalletsDestinations (M, π_k) . Then, the pallets are considered in non-descending order of $|D_i^{long}|.$

For each pallet *i*, its n_{π_k} possible edges e_{ij} are considered in nonincreasing order of θ_{ii} :

• In the greedy phase (lines 4-20), a partial solution for each pallet *i* is constructed by adding edges following θ_{ij} order. Indices η_1 and η_2 refer to the accumulated volumes $V_i \times level_1$ and $V_i \times level_2$, respectively, which were defined empirically by the *irace* tool (Lopez-Ibanez et al., 2016). We will explain this in Section 6.1.

- In the *composition phase* (lines 21–27), a set of shims named *Set* is created for each pallet *i*, where each shim is formed by a set of edges in the range $[\eta_1, \eta_2]$, whose total volume is limited by *slack_i*. In this phase, the heuristic that provided the best results, both in terms of time and quality, is based on *First-Fit Decreasing*, which is an approximation algorithm for the *Bin Packing Problem* (Johnson & Garey, 1985). Basically, shims are created by accumulating the following edges, taking *slack_i* as a limit.
- In the *selection phase* (lines 28–51), the best shim in *Set* is chosen. Initially, two shims are found: sh_w with larger weight and sh_v with larger volume. Between the two, the one with the highest score will be chosen, and its edges will be inserted into $E_{N_{\pi v}}$.

5.3. Time complexity using Shims

We finish this section with the analysis of the time complexity of our ACLP+RPDP solution, considering the use of the *Shims* heuristic.

In this process, when K > 6 (that is, in unusual cases of air transportation), we need a GA-based TSP heuristic to generate 100 tours of size *K*. This heuristic can be chosen and calibrated to be fast enough: specifically, in the tests we will present in the next section, it took just 33*s* with K = 15. For this reason, we will not perform its complexity analysis. We will also not consider the time spent by the *irace* tool, in defining parameters for *Shims*, as it is only executed once in the calibration of our method.

Let $n = \max n_k$. Without loss of generality, we assume that $m = \mathcal{O}(n)$ and therefore $\max m_k = \mathcal{O}(n)$. This way, to read the input data, Algorithm 1 requires time $\mathcal{O}(m+K^2+K.n+m.\max m_k) = \mathcal{O}(m.n)$, because K < m.

Since *ntours* \leq 6!, it is enough to calculate the complexity of Algorithm 2:

- Its initial variables are $\mathcal{O}(K.n)$.
- Algorithm 3 minimizes the CG deviation related to packed contents using a MIP solver. We are unable to analyse its time complexity, but we found that it is very fast in all cases considered in our work, where m = 18: it spent a maximum of 30 ms. The final loop of Algorithm 3 takes time O(m.n).
- Algorithm 4 takes $\mathcal{O}(n + K + m)$ time.
- Shims, described in Algorithm 6, spends $\mathcal{O}(m, \log m)$ in ordering the pallets and then performs a loop with *m* iterations. Each of these iterations spends $\mathcal{O}(n, \log n)$ on ordering the edges by the value of θ_{ij} , and $\mathcal{O}(n)$ on the others statements. So its total time is $\mathcal{O}(m.n, \log n)$.
- Algorithm 5 takes $\mathcal{O}(m.n)$ time.

Therefore, since there are *K* iterations in Algorithm 2, we can conclude that its total time is $\mathcal{O}(K.m.n.\log n)$, which is the time complexity of ACLP+RPDP solution.

6. Implementation and results

This section is composed of two parts: the generation of the test instances and the results obtained in our implementation.

6.1. Instances generation

As we are dealing with a new problem that until now had not been modelled in the literature, we have to create our own benchmarks. For this, we based it on the characteristics of real airlifts carried out by the *Brazilian Air Force*, as described below.

In the delivery of supplies carried out in Brazil from 2008 to 2010, 23% of the items weighed between 10 kg and 20 kg, 22% from 21 kg

Table 9

Item	Р	Low (kg)	High (kg)		
1	0.23	10	20		
2	0.22	21	40		
3	0.24	41	80		
4	0.23	81	200		
5	0.08	201	340		

to 40 kg, 24% from 41 kg to 80 kg, 23% from 81 kg to 200 kg, and 8% between 201 kg and 340 kg. These five groups of items are described in Table 9, where *P* represents the group probability. On the other hand, the average density of these items is approximately 246 kg/m³.

In the generation of test instances, we use two types of random selections:

- *RandomInt*(*i*₁, *i*₂): randomly selects a integer number in [*i*₁, *i*₂], where *i*₁ and *i*₂ are integer numbers;
- *Roulette(set)* biased through φ: selects an element from *set*, where the probability of each element is proportional to the value of a given function φ defined on *set*.

The procedure *ItemsGeneration*, which generates *N* (all items to be moved among the nodes), is described in Algorithm 7.

Algorithm 7 Generating items

_		
1:	ItemsGeneration in: scenario, surplus out: N	
2:	Let L be the set of nodes and M the set of pallets	
3:	$limit \leftarrow surplus \times \sum_{i=1}^{m} V_i$	
4:	for $k \leftarrow 0$ to K do	
5:	$N_k \leftarrow \emptyset$	
6:	$j \leftarrow 0$	
7:	$vol \leftarrow 0$	
8:	while vol < limit do	
9:	$j \leftarrow j + 1$	
10:	Let t_j^k be the item j at the node k	
11:	repeat	
12:	$to_j \leftarrow RandomInt(0, K)$	
13:	until $to_j \neq k$	
14:	x = Roulette(item) biased through P	⊳ From Table 9
15:	$w_j \leftarrow RandomInt(low(x), high(x))$	
16:	$s_j \leftarrow \lfloor 100 \times (1 - \log_{10}(RandomInt(1, 9))) \rfloor$	
17:	$v_j \leftarrow w_j / RandomInt(148, 344)$	
18:	$vol \leftarrow vol + v_j$	
19:	$N_k \leftarrow N_k \cup \{t_i^k\}$	
20:	end while	
	end for	
22:	$N \leftarrow \bigcup_{0 \le k \le K} N_k$	

scenario defines *L* and *M* (line 2), and the argument *surplus* sets a limit on the total volume of items at each node (line 3). To avoid simply loading all items, we use *surplus* \in {1.2, 1.5, 2.0}. This also represents more instances for tests in each scenario.

For each generated t_j^k item, its destination is randomly selected (line 12), its weight has a distribution according to Table 9 (lines 14–15), its score varies 100 (highest) and 5 (lowest) according to a logarithmic scale (line 16), and its volume is randomly defined from the density, where we allow a variation of 40% around the average density of 246 kg/m³ (line 17).

To determine the parameters $level_1$ and $level_2$ used by Shims, we previously carried out some experiments with the *irace* tool (Lopez-Ibanez et al., 2016), the results of which are presented in Table 10. In these tests, of every 7 instances generated for each value of *surplus*, 4 were used as the training set and 3 as the testing set. We provided the ranges [0.8, 1.0] and [1.0, 2.0] for $level_1$ and $level_2$, respectively. In each experiment, there was a maximum of 3000 runs so that *irace* would have enough data for its statistical tests. For more details, see cran.r-project.org/web/packages/irace/.

Table 10

irace results.											
Surplus	$Level_1$	$Level_2$	Runtime (min)								
1.2	0.8621	1.0539	47								
1.5	0.9199	1.1399	59								
2.0	0.9617	1.5706	63								

Overall result	S.		
Method	Best scenarios	Worst scenarios	Worst runtimes (min)
NMO	4	5	60
ACO	2, 3	4, 5	25, 61
GRASP	1	4, 5	28, 55
TS	-	5	44
GA	-	1, 2, 3, 4, 5	Did not solve
Gurobi	1, 2, 3, 4	5	Did not solve
Shims	1, 2, 3, 4, 5	-	3.26

6.2. Obtained solutions: quality and runtimes

In the tests performed, we used a 64-bit, 16 GB, 3.6 GHz, eightcore processor with *Linux Ubuntu 22.04.1 LTS 64-bit* as the operational system and *Python 3.10.4* as the programming language. We also used the well-known solver *Gurobi* (www.gurobi.com), version 9.5.2.

We will first present the results obtained in practical cases, when $1 < K \le 6$. Next, we will show how *Shims* remains robust when K > 6.

6.2.1. Results when $1 < K \leq 6$

We ran Algorithm 1 considering the 5 scenarios from Table 8, 3 values for *surplus* from $\{1.2, 1.5, 2.0\}$, 4 values for *tmax* from $\{240 \text{ s}, 1200 \text{ s}, 2400 \text{ s}, 3600 \text{ s}\}$, and 7 different methods for the node-by-node solution: *Gurobi* (Section 5.2.1), ACO, NMO, TS, GRASP, GA, and *Shims* (Algorithm 6).

For *Gurobi* to be able to solve the largest possible number of tests without memory overflow, we set its parameter *MIPgap* to 1%. This shortens its runtime, in addition to ensuring that its objective function f is at most 1% of the optimal solution. For more details, see https: //www.support.gurobi.com For each *scenario*, *surplus* and *tmax* tested, 7 different instances were generated.

Table 11 succinctly shows the overall performance of the methods for the node-by-node solution. Only *Shims* found a solution for all scenarios, as well as being the fastest.

Table 12 shows a particular case (*surplus* = 1.2, *ntours* = K!, and *tmax* = 3600 s) in which the methods can find solutions for all scenarios. As can be seen, *Shims* always obtained the best value for the objective function, in addition to being the fastest.

All methods used (ACO, NMO, TS, GRASP, and GA) generate a large number of solutions that require further evaluation, resulting in longer runtimes. On the other hand, *Shims* is a constructive heuristic that continually builds a feasible solution, which makes it much faster. *Shims* uses the *First-Fit Decreasing* algorithm and the *irace* tool, which follow a greedy process in the search for solution quality.

It is important to highlight that the speed of obtaining a balanced allocation at a node is essential for the ACLP+RDPD solution. Only in this way will it be possible to make the various comparisons between different routes, allowing the obtaining of an efficient flight itinerary with pickup and delivery.

Fig. 7 shows the pallet occupancy rate (weight and volume) at each tour node found by *Shims*, with *scenario* = 1, *surplus* = 1.2 and tmax = 3600 s. As can be seen, the number of pallets with a high volume rate tends to grow throughout the tour.

For these reasons, we will present only the results obtained by *Shims*, with the average of the objective function f and the runtime of *Gurobi* and *Shims*. To facilitate the comparison between both, we added a last column in the tables where two values are indicated:

- **Normalized**: value between 0 and 1, which corresponds to the ratio between the sum of *f* values obtained by the method in all scenarios and the sum of the best values obtained by both methods in all scenarios. The higher the value of **Normalized**, the closer the method approached the best solutions found.
- **Speed-up**: ratio of the sums of the runtimes of all scenarios and the sum of the method runtimes in all scenarios. The method with the highest **Speed-up** is the fastest.

We also indicate the adopted strategies: dedicating all the processing time to the *ntours* = 2 shortest tours or distributing it among all *ntours* = K! tours. The results obtained with *tmax* = 3600 s, which is the highest tested runtime limit, are in Tables 13–15, with *surplus* values of 1.2, 1.5 and 2.0, respectively. We indicate with an **x** the cases where *Gurobi* did not find a feasible solution within this runtime limit or had to be aborted due to high random-access memory (RAM) usage.

From these data, we can draw some conclusions:

- The strategy of testing all *K*! tours often provide a better-quality solution, even with less time on each node. This shows that the four sub-problems are interconnected in such a way that it is not enough to solve them separately.
- *Gurobi* fails in some cases when *scenario* = 5 and the strategy is to check all *K*! tours. This occurs because the runtime limit per node is smaller and there tend to be more packed contents on the aircraft, reducing the space for allocating items and making the solution difficult.
- When *Gurobi* finishes, it finds the best solution, but the one obtained by *Shims* reaches at least 98.96% of that value. Considering only the strategy of testing all *K*! tours, this value increases to 99.58%.
- Shims always finds a solution, being 7 to 40 times faster.
- All runtimes are much lower than the limit because the solution on many nodes can be fast. Anyway, in all the tests performed, the maximum time spent by *Shims* did not reach 4 min. On the other hand, when *scenario* = 5 and *surplus* = 1.5, *Gurobi* spent almost 40 min.

Table 16 shows the results obtained with the strategy of testing the K! tours in all scenarios with different *tmax*. We can observe more cases where *Gurobi* fails, even in smaller scenarios. When *Gurobi* finishes, *Shims* finds a solution of similar quality (99% or better). In all cases, *Shims* finds a solution in less than 4 min.

The actual RAM consumption of *Gurobi* was over 8.5 GB, and all of *Shims* 's executions consumed at most 1.5 GB of RAM.

Table 12 Solutions with surplus = 1.2, ntours = K!, and tmax = 3600 s.

Scenario	NMO		ACO		GRASP	GRASP		TS			Shims	
	f	Time (s)										
1	8.38	4	8.40	17	8.40	12	8.39	4	5.03	154	8.49	1
2	11.21	17	11.29	56	11.24	47	11.12	18	5.66	544	12.10	2
3	13.12	87	13.25	278	13.13	258	13.03	90	5.63	2,614	13.30	8
4	13.32	520	13.73	1,516	13.31	1,690	13.22	586	5.45	2,924	14.49	10
5	52.20	3,582	52.36	3,602	52.16	3,292	51.21	2,627	18.74	3,192	53.61	36

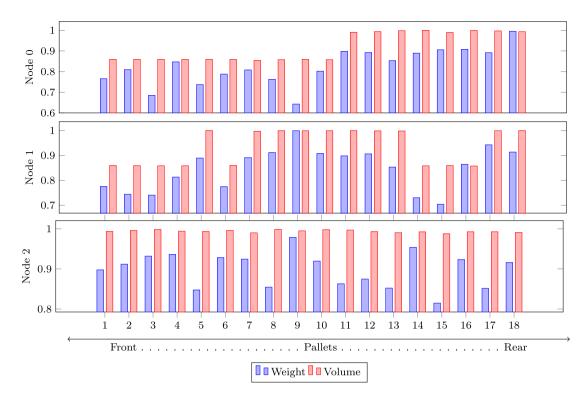


Fig. 7. Occupation rates obtained by Shims with scenario = 1, surplus = 1.2 and tmax = 3600 s.

Table 13Solutions with surplus = 1.2 and tmax = 3600 s.

ntours	Method	Scenario	1	2	3	4	5	Normalized speed-up
2	Gurobi	f Time (s)	8.53 29	11.79 28	13.14 25	13.52 27	x x	0.9998 1.0
2	Shims	f Time (s)	8.54 1	11.78 1	13.06 1	13.51 1	48.47 2	0.9980 22.7
<i>K</i> !	Gurobi	f Time (s)	8.60 30	12.20 35	13.66 123	15.00 314	x x	0.9998 1.0
K!	Shims	f Time (s)	8.49 1	12.10 2	13.30 8	14.49 10	53.61 36	0.9958 7.49

ntours	Method	Scenario	1	2	3	4	5	Normalized Speed-up
2	Gurobi	f Time (s)	11.83 55	16.73 64	18.07 39	18.83 40	16.86 88	0.9996 1.0
	Shims	f Time (s)	11.85 1	16.72 1	18.05 2	18.80 2	16.87 2	0.9993 35.8
<i>K</i> !	Gurobi	f Time (s)	11.83 63	16.93 59	18.40 195	20.95 472	17.60 2,258	0.9999 1.0
	Shims	f Time (s)	11.85 1	16.91 2	18.36 5	20.93 15	17.50 100	0.9976 23.8

6.2.2. Results when K > 6

These last results do not correspond to practical cases of air transport, as tours where K > 6 very rarely occur. However, it is possible to see that the *Shims* maintains robust behaviour as the number of nodes grows, that is, it could be adapted to similar contexts (ships and trucks, for example), where there may be more nodes.

Considering real data from the 15 main Brazilian airports, we implemented a GA-based TSP heuristic that returned 100 tours in

approximately 33 s. We implemented this heuristic with DEAP (Distributed Evolutionary Algorithms in Python), an evolutionary computation framework. For more details, see Fortin et al. (2012) and github.com/deap/deap.

Fig. 8 shows the runtime curve of *Shims* as the number *K* of nodes increases. Runtime is the average obtained from 7 instances generated with *surplus* = 2.0 and *tmax* = 1200 s for each value of *K*. In Fig. 9, we indicate one of the tours found by this TSP heuristic when K = 15.

Solutions	with <i>surplus</i>	= 2.0 and tma	x = 3600 s.					
ntours	M ethod	Scenario	1	2	3	4	5	Normalized speed-up
2	Gurobi	f Time (s)	17.70 168	24.20 98	26.39 79	27.17 70	24.20 72	0.9995 1.0
-	Shims	f Time (s)	17.74 1	24.22 2	26.32 2	27.07 3	23.13 4	0.9896 40.6
<i>K</i> !	Gurobi	f Time (s)	17.90 178	25.44 143	26.51 378	29.13 862	x x	0.9994 1.0
	Shims	f Time (s)	17.94 1	25.45 3	26.44 10	28.84 31	26.22 196	0.9970 34.7

Solutions testing all K! tours with different runtime limits.

	surplus		1.2					1.5					2.0				
Method	tmax	Scenario	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
	240 s	f	8.60	12.20	13.67	x	x	11.77	16.38	18.10	x	x	17.89	25.42	x	x	x
Gurobi	240 S	Time (s)	31	35	124	х	х	52	59	200	x	x	188	145	x	x	x
	1000 -	f	8.61	12.20	13.31	10.00	x	11.77	17.02	18.25	20.64	x	17.75	25.24	26.49	27.97	x
	1200 s	Time (s)	28	37	129	320	x	46	61	190	304	x	161	139	384	579	x
	0.400 -	f	8.60	12.21	13.67	15.00	13.41	11.77	16.37	18.03	20.95	x	17.89	25.44	26.15	29.13	x
	2400 s	Time (s)	26	38	134	310	1,520	46	60	199	461	x	164	140	383	786	x
	2600 -	f	8.60	12.20	13.66	15.00	x	11.76	16.37	18.01	20.95	17.60	17.90	25.44	26.15	29.13	x
	3600 s	Time (s)	30	35	123	314	x	64	58	195	472	2,258	178	143	378	862	x
Shims 2	0.40	f	8.49	12.10	13.30	14.49	53.61	11.78	16.29	17.99	20.93	17.50	17.94	25.45	26.14	28.84	26.22
	240 s	Time (s)	1	2	8	10	36	1	2	5	15	100	1	3	10	31	196

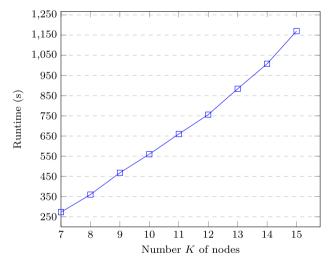


Fig. 8. Shims performance with surplus = 2.0 and tmax = 1200 s.



Fig. 9. A tour where K = 15.

7. Conclusions

In this work, we modelled and solved a real air transport problem named *Air Cargo Load Planning with Routing, Pickup, and Delivery Problem* (ACLP+RPDP). For the first time in the literature, a *NPhard* problem that involves *simultaneously* pallet assembly, load balancing, route planning, and pickup and delivery is addressed, where the cost-effectiveness of transport is maximized. Currently, there is no commercial software available for this problem.

We adopted some simplifications that are not critical, but that allowed for an unprecedented solution to this problem considering several nodes. In practical cases, there are hundreds of items to be shipped at each node, and the number of nodes, excluding the base, is smaller than the number of pallets. Considering a real aircraft, we have developed node-by-node solutions such that the complete process can be executed quickly on a handheld computer, offering good results and reducing stress for the transport planners. As validation, we carried out tests in several scenarios. In the real cases, the solution process can establish, in less than four minutes, a flight itinerary for a single aircraft with a good distribution of load on pallets at each node of the tour, enforcing the weight balance, maximizing the total score, and minimizing fuel consumption along the planned route, which is beneficial to reduce carbon emissions. This output is an essential part of airlift: it guarantees flight safety, makes ground operations more efficient, and makes sure that each item gets to its right destination.

Our main contributions were the mathematical modelling of ACLP+RPDP, involving four well-known and interconnected *NP-hard* sub-problems, a complete process to solve it, and a new heuristic named *Shims* that offers fast node solutions with good quality. Without a quick method for balanced allocation at each node, it would be unfeasible to find a flight itinerary and, consequently, a pickup and delivery plan on this tour.

We also show that this solution process remains valid in other contexts where there may be a greater number of nodes. This way, our method is not exclusive to aircraft and airports: it can be adapted to ships and ports, trucks and warehouses, or wagons and railways. In these situations, it would be necessary to make some changes in the model: for example, modify the load balancing constraints and consider parts of the available space as pallets.

As this is ongoing research, we thought about some possible future improvements: consider more than one aircraft, implement parallel algorithms in some steps of the solution to improve computational efficiency, and model 3-D items.

CRediT authorship contribution statement

A.C.P. Mesquita: Conceptualization, Methodology, Software, Writing – original draft, Investigation, Validation. **C.A.A. Sanches:** Conceptualization, Methodology, Resources, Supervision, Writing – review & editing.

Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Carlos Alberto Alonso Sanches reports financial support was provided by São Paulo Research Foundation (FAPESP). If there are other authors, they declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The dataset and code used in this work are available in github.com/ celiomesquita/ACLP_RPDP_P.

Acknowledgements

This research was partially supported by the São Paulo Research Foundation (FAPESP), Brazil, grant 2022/05803-3.

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